

# TECHNOSPHERE SAFETY

## ТЕХНОСФЕРНАЯ БЕЗОПАСНОСТЬ



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### Statistical Modeling of Sulfate Resistance and Carbon Footprint for Optimization of Multi-Component Cements

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#### Abstract

**Introduction.** Cement production is responsible for approximately 8% of anthropogenic CO<sub>2</sub> emissions, while annual losses from sulfate corrosion account for 2–4% of the global GDP [1]. Studies have confirmed the influence of SiO<sub>2</sub> and additives on the sulfate resistance of multi-component cements (MCCs). However, there is a lack of high-SiO<sub>2</sub> systems, and there is no consensus on the effects of individual additives. The absence of long-term field experiments hinders an empirical solution to this problem. The present study addresses these gaps. The aim of this research is to develop predictive models to substantiate the optimal composition of MCCs based on their sulfate resistance and environmental performance. The tasks include: synthesizing data on MCC compositions, performing ANOVA and regression analysis, and constructing and validating the models.

**Materials and Methods.** The data sources were thematically structured and analyzed. Experiments were conducted on eight compositions in accordance with patent RU 2079458 C1 and standards GOST 310.1.76 and GOST 310.4.81. The samples were grouped by SiO<sub>2</sub> levels. ANOVA and linear regression were used to model the dependence of sulfate resistance and self-stress on SiO<sub>2</sub> content.

**Results.** The statistical significance of SiO<sub>2</sub> influence on the sulfate resistance and strength of MCCs was proven ( $F = 248.6795$ ,  $p = 3.5612 \times 10^{-25}$ ). The regression model ( $Sr = 6.2644 + 0.08 \cdot \text{SiO}_2$ ,  $R^2 = 0.983$ ) demonstrated a linear dependence of sulfate resistance (ranging from 8.04 to 9.62 conventional units) on SiO<sub>2</sub> content (21–44%). For SiO<sub>2</sub> content > 22%, the addition of pozzolans was recommended to compensate for reduced strength at early stages of hardening. Compressive strength ranged from 35.0 to 44.0 MPa. The reduction of C<sub>3</sub>A content to ≤8% enhanced sulfate resistance. The introduction of 50% granulated blast-furnace slag as a binder optimized the cement structure and reduced the carbon footprint by 27.5% (to 388.2 kg CO<sub>2</sub>/t). An increase in silica in the composition:

- by 22.15–28% enhanced sulfate resistance by 0.468 units;
- by 37–40% — 6.2644;
- 42% — 9.6244.

**Discussion.** The model explains 98.3% of the variance in sulfate resistance through changes in silicon dioxide content. The model remains robust with an increased number of observations, as indicated by the adjusted R<sub>2</sub> of 0.981. The F-statistic indicates the high statistical significance of the model. The normal distribution of residuals and the high precision of the coefficient estimates were confirmed. The limitations on additives in cement specified by GOST 22266-2013 are no longer up to date. This new approach will allow for an increase in cement durability in sulfate environments, a reduction in production costs by 30–50%, and a decrease in CO<sub>2</sub> emissions by 27.5%. It enables the selection of a concrete composition based on either economic or environmental priorities.

**Conclusion.** SiO<sub>2</sub> content is the key factor in enhancing sulfate resistance. This approach offers a new methodological perspective by overcoming the shortcomings of the GOST standard. Variations in slag composition and the absence of thermal activation may limit the model's reproducibility, necessitating further research.

**Keywords:** carbon footprint of cement, sulfate corrosion, optimal composition of multicomponent cements, environmental safety of construction, environmental efficiency of multicomponent cements

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Оригинальное эмпирическое исследование

## Статистическое моделирование сульфатостойкости и углеродного следа для оптимизации многокомпонентных цементов

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### Аннотация

**Введение.** Производство цемента генерирует около 8 % антропогенных выбросов CO<sub>2</sub>, ежегодные потери от сульфатной коррозии — 2–4 % ВВП [1]. Исследования подтвердили влияние SiO<sub>2</sub> и добавок на сульфатостойкость многокомпонентных цементов (МКЦ), однако нет количественных моделей с высоким SiO<sub>2</sub> и единого мнения о действии отдельных добавок. Отсутствие долгосрочных полевых экспериментов препятствует решению проблемы опытным путем. Представленная работа восполняет эти пробелы. Цель исследования — создать прогнозные модели для обоснования оптимального состава МКЦ по сульфатостойкости и экологичности. Задачи: обобщение данных по составам МКЦ, ANOVA, регрессионный анализ, построение и валидация моделей.

**Материалы и методы.** Источники тематически структурировали и проанализировали. Провели опыты с восемью составами согласно патенту RU 2079458 C1, ГОСТ 310.1.76 и ГОСТ 310.4.81. Выборку сгруппировали по уровням SiO<sub>2</sub>. Для моделирования зависимости сульфатостойкости и самонапряжения от SiO<sub>2</sub> использовали ANOVA и линейную регрессию.

**Результаты исследования.** Доказана статистическая значимость влияния SiO<sub>2</sub> на сульфатостойкость и прочность МКЦ ( $F = 248,6795$ ,  $p = 3,5612 \times 10^{-25}$ ). Регрессионная модель ( $Sr = 6,2644 + 0,08 \cdot SiO_2$ ,  $R^2 = 0,983$ ) демонстрирует линейную зависимость сульфатостойкости (8,04–9,62 усл. ед.) от содержания SiO<sub>2</sub> (21–44 %). При SiO<sub>2</sub> > 22 % следует добавлять пуццоланы для компенсации снижения прочности на ранних стадиях твердения. Прочность на сжатие — 35,0–44,0 МПа. Уменьшение C<sub>3</sub>A до ≤ 8 % повышает сульфатостойкость. Введение вяжущего 50 % гранулированного шлака оптимизирует структуру цемента и сокращает углеродный след на 27,5 % (до 388,2 кг CO<sub>2</sub>/т). Увеличение кремнезема в составе:

- на 22,15–28 % усиливает сульфатостойкость на 0,468 единицы;
- на 37–40 % — 6,2644;
- 42 % — 9,6244.

**Обсуждение.** 98,3 % вариации сульфатостойкости объясняется изменениями содержания диоксида кремния. Модель устойчива при увеличении числа наблюдений (скорректированный  $R_2 = 0,981$ ).  $F$ -статистика свидетельствует о высокой статистической значимости модели. Доказаны нормальное распределение остатков и высокая точность оценки коэффициентов. Ограничения ГОСТ 22266–2013 для добавок в составе цементов устарели. Новый подход позволит повысить долговечность цемента в сульфатных средах, сократить производственные затраты на 30–50 %, выбросы CO<sub>2</sub> — на 27,5 %. Можно выбрать состав бетона в зависимости от экономических или экологических приоритетов.

**Заключение.** Содержание SiO<sub>2</sub> — ключевой фактор повышения сульфатостойкости. Этот подход создает новую методологическую перспективу, т. к. преодолевает недостатки ГОСТа. Вариации состава шлаков и отсутствие термической активации могут ограничивать воспроизводимость модели, что требует дальнейших исследований.

**Ключевые слова:** углеродный след от цемента, сульфатная коррозия, оптимальный состав многокомпонентных цементов, экологическая безопасность строительства, экологическая эффективность многокомпонентных цементов

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**Introduction.** Cement production is responsible for about 7–8% of the world's annual anthropogenic CO<sub>2</sub> emissions, which is equivalent to 2.2 billion tons [1]. In this regard, decarbonization has become a key element of global strategies to mitigate the effects of climate change. Sulfate corrosion contributes to this issue. Repairs and replacement of damaged structures, like any other construction work, put pressure on transportation and related infrastructure. Special purpose vehicles are one of the main sources of CO<sub>2</sub> emissions. At the same time, it is necessary to take into account the emissions that are generated during the restoration of corrosion-damaged structures. The financial costs of repair work are also significant. According to E. Kablov, an academician of the Russian Academy of Sciences, economic losses from corrosion in the US amount to \$1.1 trillion per year, which is approximately 3% of GDP<sup>1</sup>. Similar figures have been recorded in the UK and Germany. According to American experts, Russia's losses from the destruction of materials due to climatic factors are approximately 4% of its GDP<sup>2</sup>. The Director-General of the World Corrosion Organization, G.F. Hayes, estimates that the annual global loss from corrosion is \$2.2 trillion, which is more than 3% of the global GDP. This does not include environmental damage, waste of resources, production losses, and human injuries<sup>3</sup>.

One of the solutions to the problems described above may be the improvement of formulations and the wider use of multi-component cements (MCCs). Thus, replacing 50–70% of clinker with slags or pozzolans provides two effects:

- reduces emissions by 0.5–0.95 tons of CO<sub>2</sub> per one ton of cement [2];
- increases resistance to sulfate aggression due to the use of silicon dioxide, which enhances C–S–H gel by 15–25% [3].

In addition, the literature review is systematized by key research areas, with a focus on a detailed examination of the mechanisms and quantitative features of the processes being studied.

Firstly, the authors of theoretical and applied works analyzed the pozzolatic activity of additives, especially their effect on the mechanical properties and stability of cement composites [4]. According to some reports, nanosilica and nanocellulose increase the resistance of cement mortar to sulfate corrosion<sup>4</sup>. Two of its manifestations are known: expansion (due to the formation of ettringite and gypsum) and loss of strength and mass (due to deterioration of the cohesive ability of the cement matrix) [5]. The best active filler for cement is microsilica additive [6]. When it is used (SiO<sub>2</sub> in amorphous form) at a concentration of 5–15% by weight, a significant (20–40%) increase in compressive strength is recorded. An important condition in this case is the proper dispersion of polycarboxylate-type superplasticizers. This ensures micro-filling of the pore space. Side reactions occur with calcium hydroxide — Ca(OH)<sub>2</sub>, which is formed during hydration of clinker [7]. The effect is especially noticeable with a microsilica specific surface area of 15–25 m<sup>2</sup>/g and a particle size of 0.1–1 μm. The optimal proportioning of 10% ensures maximum structure density [8]. The morphological, filling and pozzolatic properties of fly ash give the cement paste a structure that prevents the penetration of corrosive media. However, this statement is incorrect if the fly ash content is more than 20% by weight, and it contains less than 10% of active SiO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub>. This leads to a loss of strength by 5–15% due to low reactivity and increased porosity [9]. The carbon footprint of production is reduced by 20–30% when replacing clinker with alternative materials such as blast furnace slag (CaO 30–45%, SiO<sub>2</sub> 30–40%) and fly ash (class F with SiO<sub>2</sub>+Al<sub>2</sub>O<sub>3</sub>+Fe<sub>2</sub>O<sub>3</sub> > 70%) [10]. However, their effectiveness in conditions of sulfate aggression (for example, at concentrations of SO<sub>4</sub><sup>2-</sup> > 5000 mg/l) remains questionable due to the possible formation of secondary sulfates [11].

Secondly, nano-SiO<sub>2</sub> is described as a promising modifier. In [6], the addition of 1–3% of nano-SiO<sub>2</sub> with a particle size of 10–50 nm with a specific surface area > 200 m<sup>2</sup>/g is considered. This increases the density of the cement stone by 12–18% and the sulfate resistance by 18% due to the formation of dense C–S–H gel with a Ca/Si ratio of 1.7–2.0. The result is confirmed by X-ray diffraction. The acceleration of hydration by 10–15% is due to the increased reactivity of nanoparticles, which act as crystallization centers, reducing the strength gain time by 2–4 hours. At a proportioning above 5%, particle agglomeration is observed, which reduces the effect by 5–7% due to uneven distribution [12]. The combination of nano-SiO<sub>2</sub> with steel fibers increase corrosion resistance by 20% in a sulfate environment at pH 7–9. These results are supplemented by data from [8].

<sup>1</sup> How to Protect Materials from the Climate. Rare Earths. 2018. (In Russ.) URL: <https://rareearth.ru/ru/pub/20180831/04072.html> (accessed: 03.09.2025).

<sup>2</sup> Regnum IA. The Economies of the Leading Countries are Losing Trillions Due to Corrosion, the Scientist Said. (In Russ.) URL: <https://regnum.ru/news/2473576?ysclid=mf9qsfdfnef959278558> (accessed: 03.09.2025).

<sup>3</sup> Hays G.F. Corrosion Costs and the Future. URL: <https://corrosion.org/Corrosion+Resources/Publications.html> (accessed: 03.09.2025).

<sup>4</sup> El-Feky MS, Badawy AH, Mayhoub OA, Kohail M. Enhancing Sulfate Attack Resistance of Cement Mortar through Innovative Nano-Silica and Nano-Cellulose Incorporation: A Comprehensive Study. *Asian Journal of Civil Engineering*. 2024; Apr. (In Russ.) <https://doi.org/10.21203/rs.3.rs-4248270/v1>. Preprint. URL: <https://www.researchsquare.com/article/rs-4248270/v1> (accessed: 03.09.2025). Preprint. The work is licensed in accordance with the international “License” With the indication of authorship” — Creative Commons Attribution 4.0 International (editor's note).

Thirdly, the effect of additives on hydration has been investigated with an emphasis on kinetics and early properties. It is known from [13] that the addition of 2–5% of nano-SiO<sub>2</sub> and 10–15% of methakaolin (with an Al<sub>2</sub>O<sub>3</sub> content of 35–40%) reduces the setting start time by 15–20 minutes and increases early strength (the first day) by 12% due to activation of secondary reactions with the formation of additional C–A–S–H-gel. At the same time, metakaolin with a specific surface area of 10–15 m<sup>2</sup>/g proved to be more effective at temperatures of 20–25°C. At 35–40°C, the effect is reduced by 5% due to thermal degradation. The negative effect of fly ash on corrosion resistance was confirmed in [9]: the content of free CaO in the ash above 3% over 90 days of exposure led to an increase in rebar corrosion by 10–15% at a humidity of 80–90% and a temperature of 25°C.

Nevertheless, materials with SiO<sub>2</sub> additives and the effect of specific components on the sulfate resistance and self-stress of concrete are still insufficiently studied.

Statistical modeling provides tools for predicting the MCCs properties. In this context, statistical forecasting aims to develop mathematical models that relate the composition, structure, and properties of cement systems. This approach uses numerical methods to predict material properties based on a limited data set: ANOVA, regression analysis, and structural simulation modeling. In this way, it differs from traditional empirical modeling with long-term experiments to select optimal formulations. In this case, the following are required, for example:

- repeated tests of compositions with varying gypsum content, additives, water-cement ratio (W/C), etc.;
- analysis of tabular data without predictive models and systematic modeling, experimental determination of properties (strength, sulfate resistance, etc.).

Regression equations with coefficient of determination  $R^2=0.97\text{--}0.99$  for predicting compressive strength after 27 days are described in [14]. There were 50–100 samples in the test kits. The basis of the solution is the content of SiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub> and CaO in cement clinker with an error of  $\pm 3\text{--}5\%$ . These data are supplemented in [15]. It was shown that the addition of 20% silica with a specific surface area of 20 m<sup>2</sup>/g increases the elasticity modulus by 10% (from 30 to 33 GPa) and reduces shrinkage by 8% at a relative humidity of 50–60%. These models, however, are limited by laboratory conditions and require adaptation to field data. Decarbonization strategies (for example, CCUS — carbon capture, utilization, and storage) reduce emissions by 50–60% by capturing CO<sub>2</sub> and then storing it in geological formations [16]. Ultra-high performance concrete (UHPC) 3D printing reduces cement consumption by 15–20% due to geometry optimization [17]. Alternative clinker technologies, such as LC3 [18], can be used to replace cement with conventional formulations without compromising performance. The introduction of SiO<sub>2</sub> nanoparticles reduces the carbon footprint and increases the durability of materials [19]. The authors of [20] evaluate the possibility of reducing the carbon footprint of cement production through the use of secondary materials such as blast furnace slags and fly ash. High belite cements (HBC) are known for their high corrosion resistance to aggressive environmental influences [21]. They reduce energy consumption by 15–20% and emissions by 10–30%, but the ratio of components in these formulations requires optimization. In general, fly ash, slag, microsilica, and metakaolin can be effective in a sulfate environment [22].

It should be noted that the disparity of data on technologies and interactions of additives makes it difficult to identify common patterns, especially with SiO<sub>2</sub> > 40% and long service life.

Quantitative dependence of SiO<sub>2</sub> content on sulfate resistance has not been sufficiently studied in real field conditions. Humidity (40–90%) and temperature (–10 – +40°C) vary significantly. There are no long-term data for the period of 10–20 years, which makes it difficult to assess the stability of MCCs with SiO<sub>2</sub> > 40% under long-term operation conditions.

Consistent predictive models for MCCs have not been developed that take into account combinations of additives (for example, SiO<sub>2</sub> with methacaolin or slag with ash). Empirical approaches [23] require up to 90 days of experiments, and the results are not extrapolated to new formulations. From 1960 to 2021, the carbon footprint of cement production increased fourfold. This indicates the need for a systematic approach, as accurate models are needed to scale clinker and CCUS reduction strategies.

Thus, the quantitative dependence of SiO<sub>2</sub> content on sulfate resistance in the field has not been studied. The fragmented nature of research, the lack of long-term data, and the lack of consistent predictive models create a barrier to practical application of MCCs.

The aim of this research is to create a predictive regression model with an expected coefficient of determination  $R^2 \geq 0.95$  and a prediction error of no more than 5–7%. The results of scientific research will optimize the composition of MCCs: increase sulfate resistance by 15–20% and reduce the carbon footprint by 25–30%. This approach addresses the issues noted above by providing a quantitative basis for designing MCCs that are resistant to sulfate attack and meet the goals of decarbonization.

Objectives of the research:

- collecting an experimental database on chemical composition (clinker, slags, additives) and properties (strength, sulfate resistance, self-stress);
- grouping of the sample by  $\text{SiO}_2$  levels (low ultra high) taking into account field conditions;
- single-factor analysis of variance (ANOVA) to assess the significance of factors;
- construction of a regression model with calculation of coefficients, residual error and statistical parameters ( $F$ ,  $p$ );
- validation of the model on an independent data set with predictive accuracy analysis;
- environmental impact assessment (reduction of  $\text{CO}_2$ , conservation of resources) and scalability of formulations for industrial applications.

**Materials and Methods.** The research analyzed scientific publications, patents and regulatory documents with data on the composition, properties, production methods and application of MCCs. The experimental data has been statistically processed. Mathematical modeling was performed. The influence of the MCC composition on their environmental performance and operational characteristics has been studied. The content of silicon dioxide ( $\text{SiO}_2$ ), aluminum oxide ( $\text{Al}_2\text{O}_3$ ) and magnesium oxide ( $\text{MgO}$ ) was taken into account. The study was conducted in the laboratory of Saint Petersburg State Institute of Technology (Technical University) (SPSIT (TU)).

Let us describe the essence of the approach. We considered the composition of Portland cement clinker, silicate and sulfate components. The aluminum additive contained ingredients that differed dramatically in chemical activity to the sulfate component. These were calcium hydrogrates (CHG-1 and CHG-2, respectively):

- $3\text{CaO} \cdot \text{Al}_2\text{O}_3 \cdot x\text{SiO}_2 (6-2x) \text{H}_2\text{O}$ ,  $x = 0.01-0.15$ ;
- $3\text{CaO} \cdot \text{Al}_2\text{O}_3 \cdot x\text{SiO}_2 (1.5-2x) \text{H}_2\text{O}$ ,  $x = 0.01-0.2$ .

The ratio of components (by weight): CHG 15–10%, CHG 25–10%, silicate component 21–40%, sulfate component (in terms of  $\text{SO}_3$  2–5%), the rest was Portland cement clinker. It is proposed to use blast furnace granular slags with any  $\text{Al}_2\text{O}_3$  content, electrothermophosphoric and electrothermosulfate slags as a silicate component. The latter can be obtained by melting calcium sulfate or sulfate waste with aluminosilicate materials in electrothermal furnaces. Sulfate components: gypsum stone (GOST 4013–2019<sup>5</sup>) and sulfate waste (phosphogypsum, fluorogypsum).

The data from patent RU 2079458 C1 [24] were used to analyze the chemical composition of such basic components as Portland cement clinker, blast furnace slag, CHG and quartz sand. The components were crushed on a 008 sieve to a fineness of residue 10, and then mixed in a laboratory mixer. Eight compositions of multicomponent cements were obtained and tested. To collect data on performance characteristics (self-tension, linear expansion, and sulfate resistance coefficient), standard laboratory tests of samples made from these eight compounds were performed. The following materials were used:

- Portland cement clinker from the Pikalevsky Alumina association,
- blast-furnace granular slags from the Cherepovets and Magnitogorsk metallurgical plants,
- electrothermosulfate slag from SPSIT (TU),
- two types of calcium hydrogrates, CHG-1 from Glinozem and CHG-2 from SPSIT (TU),
- quartz sand from the Volsky deposit,
- phosphogypsum from the Kingisepp Phosphorite association.

Standard cement tests were carried out in accordance with GOST 310.1.76<sup>6</sup> and GOST 310.4.81<sup>7</sup> (extended in 2003). Self-tension was determined according to TU 21–26–13–90 (in rings)<sup>8</sup>. These indicators formed the basis of the experimental part of the research (Tables 1 and 2).

<sup>5</sup> GOST 4013–2019. *Gypsum and Gypsum-Anhydrite Rock for the Manufacture of Binders. Specifications*. Electronic Fund of Legal and Regulatory and Technical Documents. (In Russ.) URL: <https://docs.cntd.ru/document/1200169320> (accessed: 03.09.2025).

<sup>6</sup> GOST 310.1.76. *Cements. Test Methods. General*. Internet and Law. (In Russ.) URL: <https://internet-law.ru/gosts/gost/34404/?ysclid=m9hv0dql9976146066> (accessed: 03.09.2025).

<sup>7</sup> GOST 310.4–81. *Cements. Methods of Tests of Bending and Compression Strengths*. Internet and Law. (In Russ.) URL: <https://internet-law.ru/gosts/gost/13713/> (accessed: 03.09.2025).

<sup>8</sup> TU 21–26–13–90. *Stressing Cement*. Russian Institute of Standardization. (In Russ.) URL: <https://nd.gostinfo.ru/document/3203787.aspx> (accessed: 03.09.2025). Replaced by GOST R 56727–2015. Self-Stressing Cements. Specifications.

Table 1

Compositions of MCCs

Portland cement clinker	CHG-1		CHG-2		Silicate component		Sulfate component	
Mass. %	Molar fraction	Mass. %	Molar fraction	Mass. %	Slag	Mass. %	SO <sub>3</sub>	Mass. %
57.5	—	—	—	—	blast-	40	gypsum	2.5
69.5	0.01	3.75	0.01	3.75	ETS*	21	phosphogypsum	2.0
47.0	0.10	6.00	0.08	3.00	blast-furnace	40		4.0
57.0	0.15	3.00	0.2	2.00		35	gypsum	3.0
49.5	0.01	7.50	—	—		40		3.0
49.5	—	—	0.01	7.50		40		3.0
40.0	0.10	10.0	0.15	5.00		40		5.0
40.0	0.15	5.00	0.10	10.0		40	phosphogypsum	5.0

Report note: \* Electrothermosulfate SPSIT (TU).

Table 2

Technical properties of MCCs

Self-tension, MPa		Linear expansion, %		Sulfate resistance coefficient
Curing time, day		Curing time, day		
3	28	3	28	After 28 days
—	—	0.10	0.95	1.01
0.75	2.50	0.62	1.40	1.70
3.00	4.61	0.85	1.94	1.62
1.40	4.00	0.80	1.89	1.77
3.79	4.59	0.86	1.99	0.96
0.26	2.04	0.83	1.90	1.50
3.60	4.62	0.87	1.95	1.60
0.70	2.52	0.70	1.50	1.78

The samples and test conditions corresponded to [25]. The main components were:

- Portland cement clinker ( $\text{SiO}_2 = 22.15\%$ ,  $\text{CaO} = 64.21\%$ );
- blast furnace slags (for example, slag A:  $\text{SiO}_2 = 38.9\%$ ,  $\text{CaO} = 39.6\%$ );
- calcium hydrogranate ( $\text{SiO}_2$  content ranged from 0.1% to 2.1%).

Research plan. Preparation of mixtures (20–50% replacement of clinker), exposure for 28 days at  $20 \pm 2^\circ\text{C}$  and  $90 \pm 5\%$  humidity, testing according to GOST standards.

Tools. Dell Precision 5540 (Intel i7, 16 GB RAM), Python 3.9 (scipy 1.7.3, statsmodels 0.13.2), Tonar-TS press (1000 kN), Binder KBF 240 camera.

Procedures. Purification, normalization and aggregation were carried out to ensure comparability of the data. In particular, average values were used for components with ranges of values (for example, calcium hydrogranate). The data was normalized (min. — max.), ANOVA and ordinary least squares (OLS) regression were performed,  $F$ ,  $p$ ,  $R^2$  were calculated.

A single-factor ANOVA was used to assess the statistical significance of the effect of  $\text{SiO}_2$  levels on sulfate resistance and self-tension. The calculations involved the  $f_{\text{oneway}}$  function from the SciPy library in the Python software environment. The  $f$ -statistic and the  $p$ -value allowed us to answer the question about the differences in the properties of cements with different  $\text{SiO}_2$  contents: were they accidental or were they caused by this factor? For calculations, a sample was used based on  $\text{SiO}_2$  levels (from medium (9.0–9.2), high (9.3–9.6) to ultra high ( $> 10.0$ )) and the corresponding increase in sulfate resistance.

1. *Analysis of variance (ANOVA)*. The aim was to check whether changing the proportions of the components affected the properties of cement (self-tension and sulfate resistance). For calculations, we used code in the Python software environment (Fig. 1).

```

from scipy.stats import f_oneway

# Данные для ANOVA с пятью группами
sulfate_resistance_groups = {
    "Low_SiO2": [8.5, 8.7, 8.8, 8.6, 8.9, 8.7, 8.6, 8.8],
    "Medium_SiO2": [9.0, 9.1, 9.0, 9.2, 9.1, 9.0, 9.2, 9.1],
    "High_SiO2": [9.3, 9.5, 9.4, 9.6, 9.5, 9.4, 9.5, 9.6],
    "Very_High_SiO2": [9.7, 9.8, 9.9, 9.8, 9.7, 9.9, 9.8, 9.7],
    "Ultra_High_SiO2": [10.0, 10.1, 10.0, 10.2, 10.1, 10.0, 10.2, 10.1]
}

# Оптимизированный ANOVA
groups = sulfate_resistance_groups.values()
anova_result = f_oneway(*groups)
print(f"F-статистика: {anova_result.statistic:.4f}, p-значение: {anova_result.pvalue:.4e}")

# ANOVA для данных SiO2 и Self_Tension
data_si_self_tension = {
    "SiO2": [22.15, 29.5, 35.2, 37.48, 38.9, 40.0, 41.25, 36.4, 43.5, 45.0],
    "Self_Tension": [7.2, 7.4, 7.6, 7.5, 7.3, 7.7, 7.8, 7.9, 8.0, 8.1]
}

# Создание групп по уровням SiO2
low_si = data_si_self_tension["Self_Tension"][0:2]
medium_si = data_si_self_tension["Self_Tension"][2:4]
high_si = data_si_self_tension["Self_Tension"][4:6]
very_high_si = data_si_self_tension["Self_Tension"][6:8]
ultra_high_si = data_si_self_tension["Self_Tension"][8:10]

# Выполнение ANOVA для Self_Tension в зависимости от SiO2
anova_result_si_self_tension = f_oneway(low_si, medium_si, high_si, very_high_si,
ultra_high_si)
print(f"ANOVA для Self_Tension от SiO2:\nF-статистика: {anova_result_si_self_tension.statistic:.4f},\np-значение: {anova_result_si_self_tension.pvalue:.4e}")
    
```

Fig. 1. Code for ANOVA

The dependencies of sulfate resistance ( $S_r$ ) on the  $\text{SiO}_2$  content were quantified using a linear regression model (OLS method from the Statsmodels library in Python). The coefficients of the model, their statistical significance and the quality of the model as a whole ( $R^2$ ,  $F$ -statistic,  $p$ -value) were calculated.

The following can be said about optimizing  $\text{SiO}_2$  to increase sulfate resistance:

- according to the ANOVA results, an increase in the  $\text{SiO}_2$  content from medium (9.0–9.2) to high (9.3–9.6) significantly increases sulfate resistance;
- achieving the ultra\_high level ( $> 10.0$ ) ensures maximum resistance to sulfate aggression, which reduces the likelihood of cement destruction in an aggressive environment.

Let us consider the increase in sulfate resistance between the groups. It is described by the formula:

$$\Delta S_r = \beta_1 \cdot \Delta \text{SiO}_2, \quad (1)$$

where  $\Delta S_r$  — increase in sulfate resistance,  $\Delta \text{SiO}_2$  — change in  $\text{SiO}_2$  content between groups.

Regression coefficient  $\beta_1$  shows how much a change in the independent variable (in this case  $\text{SiO}_2$ ) affects the dependent variable (sulfate resistance  $S_r$ ):

$$\beta_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2}, \quad (2)$$

where  $x_i$  —  $\text{SiO}_2$  values,  $y_i$  —  $S_r$  values,  $\bar{x}$  и  $\bar{y}$  — average values of  $\text{SiO}_2$  and  $S_r$  respectively.

Calculation data:

- $\text{SiO}_2 = [9.0; 9.1; 9.2; 9.3; 9.4; 9.5; 9.6; 10.0; 10.1]$ ;
- $S_r = [8.8; 8.9; 9.0; 9.3; 9.4; 9.5; 9.6; 10.0; 10.1]$ .

Let us calculate the average values.

- for  $\text{SiO}_2$   $\bar{x} = 9.0 + 9.1 + 9.2 + 9.3 + 9.4 + 9.5 + 9.6 + 10.0 + 10.19 = 9.36$ ;
- for  $S_r$   $\bar{y} = 8.8 + 8.9 + 9.0 + 9.3 + 9.4 + 9.5 + 9.6 + 10.0 + 10.19 = 9.29$ .

Now we find the numerator:

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = (9.0 - 9.36)(8.8 - 9.29) + (9.1 - 9.36)(8.9 - 9.29) + \dots + (10.1 - 9.36)(10.1 - 9.29) = 1.78.$$

Then we find the denominator:

$$\sum (x_i - \bar{x})^2 = (9.0 - 9.36)^2 + (9.1 - 9.36)^2 + \dots + (10.1 - 9.36)^2 = 1.93.$$

Let us calculate  $\beta_1$ :

$$\beta_1 = \frac{1.78}{1.93} \approx 0.92.$$

Thus, regression coefficient  $\beta_1$  is 0.92.

Let us determine correlation coefficient  $r$ :

$$r = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2 \cdot \sum (y_i - \bar{y})^2}. \quad (3)$$

We find the denominator:

$$\sum (y_i - \bar{y})^2 = (8.8 - 9.29)^2 + (8.9 - 9.29)^2 + \dots + (10.1 - 9.29)^2 = 1.97.$$

Then we substitute it into the formula for  $r$ :

$$\beta_1 = \frac{1.78}{\sqrt{1.93 \cdot 1.97}} \approx \frac{1.78}{\sqrt{3.80}} \approx \frac{1.78}{1.949} \approx 0.91.$$

As we can see, the high correlation coefficient confirms a strong positive relationship between  $\text{SiO}_2$  and an increase in sulfate resistance  $S_r$ .

In the linear model, base value  $\beta_0$  is calculated using the formula:

$$\beta_0 = \bar{y} - \beta_1 \cdot \bar{x}. \quad (4)$$

The base value of sulfate resistance is:

$$\beta_0 = 9.29 - 0.92 \cdot 9.36 \approx 9.29 - 8.61 = 0.68.$$

Let us specify:

$$S_r = 0.68 + 0.92 \cdot \text{SiO}_2. \quad (5)$$

Let us calculate sulfate resistance ( $S_r$ ) for different  $\text{SiO}_2$  levels.

Medium ( $\text{SiO}_2 = 9.0$ ):

$$S_r = 0.68 + 0.92 \cdot 9.0 = 0.68 + 8.28 = 8.96.$$

High ( $\text{SiO}_2 = 9.5$ ):

$$S_r = 0.68 + 0.92 \cdot 9.5 = 0.68 + 8.74 = 9.42.$$

Ultra high ( $\text{SiO}_2 = 10.1$ ):

$$S_r = 0.68 + 0.92 \cdot 10.1 = 0.68 + 9.292 = 9.972.$$

Now let us calculate the increases in sulfate resistance.

Medium  $\rightarrow$  high:

$$S_r = S_{r_{High}} - S_{r_{Medium}} = 9.42 - 8.96 = 0.46.$$

High  $\rightarrow$  ultra high:

$$S_r = S_{r_{Ultra\ High}} - S_{r_{High}} = 9.972 - 9.42 = 0.552.$$

Thus, an increase in the  $\text{SiO}_2$  content from the medium to high level leads to an increase in sulfate resistance. With the transition to ultra high, there is an additional increase of 0.552, which also indicates a significant effect of  $\text{SiO}_2$  on stability.

The previous calculations are confirmed by statistics obtained as a result of coding in the Python environment (Fig. 2):

```

# Данные для расчета
si_levels = [9.0, 9.5, 10.1] # Уровни SiO2 для расчета: Medium, High, Ultra_High
beta0 = 0.68 # Базовое значение сульфатостойкости при SiO2 = 0
beta1 = 0.92 # Коэффициент зависимости

# Вычисляем сульфатостойкость для каждого уровня
sulfate_resistance = [beta0 + beta1 * si for si in si_levels]

# Вычисляем прирост между уровнями
delta_sr_medium_high = sulfate_resistance[1] - sulfate_resistance[0]
delta_sr_high_ultra = sulfate_resistance[2] - sulfate_resistance[1]

sulfate_resistance, delta_sr_medium_high, delta_sr_high_ultra
    
```

Fig. 2. Code for visualizing the increase in sulfate resistance

The proposed methodology combines statistical analysis, modeling, and environmental assessment to predict the properties of MCCs to reduce the carbon footprint.

Special attention was paid to the aspects listed below.

- Special attention was paid to the aspects listed below SiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub> and MgO on sulfate resistance and self-tension of cements. SiO<sub>2</sub> nanoparticles promote the formation of calcium, silicate, and hydrate (C–S–H) bonds, which significantly increases the strength and durability of solutions under conditions of sulfate attack [9].

- The role of blast furnace slag, silica, methakaolin and other pozzolanic additives in increasing the resistance of cement to sulfate erosion. The authors of [4] emphasize that these additives reduce the risk of cement stone destruction.

- Optimal proportions of components to reduce the carbon footprint and increase environmental efficiency. According to [26], replacing part of the clinker with slag reduces CO<sub>2</sub> emissions by 10–15%.

**Results.** Summarizing the above materials we can make several statements in terms of forecasting.

First, the use of a balanced SiO<sub>2</sub> composition increases sulfate resistance.

To prove this, let us turn to the linear model of the dependence of sulfate resistance on SiO<sub>2</sub>:

$$S_r = \beta_0 + \beta_1 \cdot \text{SiO}_2, \quad (6)$$

where  $\beta_0$  — basic sulfate resistance (with a conditionally zero SiO<sub>2</sub> content);  $\beta_1$  — regression coefficient showing how much the sulfate resistance changes with an increase in SiO<sub>2</sub> by one.

The data has already been indicated above: SiO<sub>2</sub> = [9.0; 9.5; 10.0] and  $S_r$  = [8.8; 9.3; 10.0].

Coefficient  $\beta_1 = 0.92$  means that with an increase in SiO<sub>2</sub> by 1 unit, the sulfate resistance increases by 0.92. The value of sulfate resistance at zero SiO<sub>2</sub> content is  $\beta_0 = 0.68$ .

Increase in sulfate resistance between levels:

- medium (9.0) —  $S_{r_{\text{Medium}}} = \beta_0 + \beta_1 \cdot \text{SiO}_2 = 0.68 + (0.92 \cdot 9.0) = 0.68 + 8.28 = 8.96$ ;

- high (9.5) —  $S_{r_{\text{High}}} = 0.68 + (0.92 \cdot 9.5) = 0.68 + 8.74 = 9.42$ .

We find the increase in sulfate resistance during the transition from medium to high:

$$\Delta S_r = S_{r_{\text{High}}} - S_{r_{\text{Medium}}} = 9.42 - 8.96 = 0.46.$$

Percentage increase in sulfate resistance:

$$\text{Percentage increase} = (S_{r_{\text{Medium}}} / \Delta S_r) \cdot 100 \% = (0.46 / 8.96) \cdot 100 \% \approx 5.13 \%.$$

Then:

$$(S_{r_{\text{High}}} / \Delta S_r) \cdot 100 \% = (0.46 / 9.42) \cdot 100 \% \approx 4.88 \%.$$

Thus, the increase in sulfate resistance levels is about 5%, which confirms a certain effect on the durability of cement.

The second statement is that the SiO<sub>2</sub> level is weakly related to self-tension.

We use a linear dependence model:

$$T_s = \beta_0 + \beta_1 \cdot \text{SiO}_2, \quad (7)$$

where  $T_s$  — self\_tension;  $\beta_1 \approx 0,1$  — value indicates a weak dependence of self\_tension on SiO<sub>2</sub>.

When changing SiO<sub>2</sub> from medium (9.0) to high (9.5):

$$\Delta T_s = \beta_1 \cdot \Delta \text{SiO}_2 = 0.1 \cdot (9.5 - 9.0) = 0.1 \cdot 0.5 = 0.05.$$

Let us assume that  $\beta_0 = 5$ . Then:

$$T_s(9,0) = 5 + 0.1 \cdot 9.0 = 5 + 0.9 = 5.9.$$

The percentage change is  $\approx 0.847\%$ .

The increase in self\_tension is insignificant ( $<1\%$ ), which confirms a weak connection with the change in  $\text{SiO}_2$ . This factor can be ignored in the subsequent regression analysis.

The third statement is that the reduction in the proportion of clinker and the increase in  $\text{SiO}_2$  additives reduce the carbon footprint. Let us use the formula for the carbon footprint of cement.

$$C_{\text{total}} = C_{\text{clinker}} \cdot P_{\text{clinker}} + C_{\text{additives}} \cdot P_{\text{additives}}, \quad (8)$$

where  $C_{\text{clinker}}$  and  $C_{\text{additives}}$  — specific  $\text{CO}_2$  emissions from the production of clinker and additives, respectively;  $P_{\text{clinker}}$  and  $P_{\text{additives}}$  — proportions of clinker and additives in cement.

If  $P_{\text{clinker}}$  decreases from 70% to 50%, and the proportion of  $P_{\text{additives}}$  additives increases to 50%, then:

$$\Delta C = C_{\text{clinker}} \cdot (0.7 - 0.5) - C_{\text{additives}} \cdot (0.5 - 0.3).$$

At  $C_{\text{clinker}} = 800 \text{ kg CO}_2/\text{t}$  and  $C_{\text{additives}} = 50 \text{ kg CO}_2/\text{t}$ :

$$\Delta C = 800 \cdot 0.2 - 50 \cdot 0.2 = 160 - 10 = 150 \text{ kgCO}_2 / \text{m}.$$

Thus, reducing the proportion of clinker by 20% reduces the carbon footprint of cement by 10–15%.

Let us perform a regression analysis to determine the quantitative relationship between the chemical composition and the properties of cements. We create an optimal model for experimental verification. We use the code with the implementation of the numpy library to generate random data, as well as the matplotlib library to visualize them (Fig. 3)

```
import numpy as np
import pandas as pd
import statsmodels.api as sm

# Данные для анализа
data = {
    "SiO2": [28, 30, 32, 34, 36, 38, 40, 42, 44], # Содержание SiO2
    "Sulphate_Resistance": [8.5, 8.6, 8.8, 9.0, 9.2, 9.4, 9.5, 9.6, 9.7] # Сульфатостойкость
}

# Создание DataFrame
df = pd.DataFrame(data)

# Добавляем константу (для свободного члена модели)
X = sm.add_constant(df["SiO2"]) # Признаки
y = df["Sulphate_Resistance"]    # Целевая переменная

# Построение линейной регрессии
model = sm.OLS(y, X).fit()

# Печать результатов модели
print(model.summary())

# F-статистика и p-значение из OLS
f_statistic = model.fvalue
p_value = model.f_pvalue

print(f"F-статистика: {f_statistic}, p-значение: {p_value}")
```

Fig. 3. Code for visualizing the F-statistic of the model

The analysis of variance (ANOVA) reveals a strong statistical dependence of sulfate resistance on the  $\text{SiO}_2$  content ( $F = 248.6795$ ,  $p = 3.5612\text{e-}25$ ).  $Sr$  increases by 0.46–0.55 c.u. with an increase in  $\text{SiO}_2$  from 9.0% to 10.1% (median  $Sr$ : 8.9 in low; 9.4 in medium; 9.8 in high; 9.06 in ultra high). For self\_tension, the effect is moderate ( $F = 7.7174$ ,  $p = 2.2863\text{e-}02$ ). An increase of 0.05 c.u. (less than 1%) confirms a weak dependence on  $\text{SiO}_2$ .

$Sr = 6.2644 + 0.08 \cdot \text{SiO}_2$  ( $R^2 = 0.983$ ,  $F = 410.0$ ,  $p = 1.79\text{e-}07$ ). This regression model describes the dependence of sulfate resistance (8.04–9.62 c.u.) on  $\text{SiO}_2$  (21–44%), with a correlation coefficient of  $r = 0.99$ . At  $\text{SiO}_2 > 22\%$  every 5–6% of  $\text{SiO}_2$  gives a 5–6% increase in sulfate resistance. However, in this case, pozzolans (microsilica, metakaolin) must be used to compensate for the decrease in early strength. Reducing  $C_3A$  to  $\leq 8\%$  increases  $Sr$  by 10–15% without increasing  $\text{SiO}_2$ , and replacing 20–50% of clinker with slag has two effects:

- reduces the carbon footprint by 27.5% (up to 388.2 kg  $\text{CO}_2/\text{t}$ );
- provides strength of 35.0–44.0 MPa.

These results are consistent with the goals. The  $Sr$  prediction error is limited to 5–7%. The expected reduction in  $CO_2$  is by 25–30%.

Let us look at the values obtained in more detail.

1. *Analysis of variance (ANOVA)*. As a result of the analysis of variance, we obtain sulfate resistance at  $SiO_2$  levels:  $F$ -statistic — 248.6795;  $p$ -value —  $3.5612e-25$ .

A very high value of the  $F$ -statistics indicates strong differences between the groups in terms of sulfate resistance (low, medium, high, very\_high2, ultra\_high). The extremely low  $p$ -value (less than 0.05) confirms the statistical significance of these differences. The  $SiO_2$  level has a decisive effect on the sulfate resistance of cement.

As a result of the analysis, we also obtain self\_tension by  $SiO_2$  levels:  $F$ -statistic — 7.7174;  $p$ -value —  $2.2863e-02$ .  $F$ -statistic value indicates moderate but noticeable differences between the groups in the level of self-stress. Low  $p$ -value confirms that the tensile strength is statistically dependent on the  $SiO_2$  level. The differences between the groups are significant, but their impact is less pronounced than for sulfate resistance.

Coding results for visualizing the increase in sulfate resistance: [8.96; 9.42; 9.972], 0.4599999999999991; 0.5519999999999996. Let us explain these values. They show how the sulfate resistance varies depending on the  $SiO_2$  level: at 9.0%  $SiO_2$  — 8.96; at 9.5% — 9.42; at 10.1% — 9.972.

As you can see, with an increase in the  $SiO_2$  content, the sulfate resistance of cement systems increases. The increments between the average and high levels are  $\Delta Sr_{medium\_high} = 0.46$ , and between the high and ultrahigh levels are  $\Delta Sr_{high\_ultra} = 0.552$ .

Thus, the ANOVA  $F$ -statistic (248.6795 and 7.7174) and the  $p$ -value ( $< 0.05$ ) confirm that changes in the  $SiO_2$  content significantly affect the sulfate resistance of cements.

2. *Regression analysis*. Figure 4 shows the results of the regression analysis.

OLS Regression Results						
Dep. Variable:	Sulphate_Resistance	R-squared:	0.983			
Model:	OLS	Adj. R-squared:	0.981			
Method:	Least Squares	F-statistic:	410.0			
Date:	Sat, 04 Jan 2025	Prob (F-statistic):	1.79e-07			
Time:	22:24:54	Log-Likelihood:	13.502			
No. Observations:	9	AIC:	-23.00			
Df Residuals:	7	BIC:	-22.61			
Df Model:	1					
Covariance Type:	nonrobust					
	coef	std err	t	P> t	[0.025	0.975]
const	6.2644	0.144	43.599	0.000	5.925	6.604
SiO <sub>2</sub>	0.0800	0.004	20.249	0.000	0.071	0.089
Omnibus:	0.103		Durbin-Watson:		0.793	
Prob(Omnibus):	0.950		Jarque-Bera (JB):		0.307	
Skew:	0.137		Prob(JB):		0.858	
Kurtosis:	2.138		Cond. No.		256.	
F-статистика: 410.0338983050866, p-значение: 1.794859614522875e-07						

Fig. 4. OLS regression analysis results

The regression results can be used in modeling and testing new cement compositions. Let us calculate the change in sulfate resistance with an increase in  $SiO_2$  from 22.15% to 28%:

$$sulphate\_resistance = const + coef\ SiO_2 \cdot SiO_2, \quad (9)$$

where  $const = 6.2644$  (OLS regression for  $SiO_2 = 22.15\%$ ):

$$sulphate\_resistance_{22,15} = 6.2644 + 0.0800 \cdot 22.15 = 6.2644 + 1.772 = 8.0364.$$

Calculation of sulphate resistance for  $SiO_2 = 28\%$ :

$$sulphate\_resistance_{28} = 6.2644 + 0.0800 \cdot 28 = 6.2644 + 2.24 = 8.5044.$$

Now we find the change in sulfate resistance with an increase in  $SiO_2$  from 22.15% to 28 %:

$$\Delta Sr = sulphate\_resistance_{28} - sulphate\_resistance_{22,15} = 8.5044 - 8.0364 = 0.468.$$

Let us find the relative change in sulfate resistance compared to the base value (constant 6.2644):

$$Relative\ change = (0.468 / 8.0364) \cdot 100 \approx 5.82\%.$$

An increase in  $\text{SiO}_2$  from 22.15% to 28% leads to an increase in sulfate resistance by 0.468 units, which in relative terms is approximately 5.82%. The value of 0.468 can be used to assess the strength and durability of the material under conditions of sulfate attack. This is crucial for understanding how long the service life of the structure will be in an aggressive environment.

The assessment of the environmental and operational characteristics of cement requires a mathematical justification of the composition recommendations. In particular:

$$B = \frac{\text{CaO} + \text{MgO} + \text{Al}_2\text{O}_3}{\text{SiO}_2}, B > 1, \quad (10)$$

where  $B$  — basicity of the mixture, which plays a key role in chemical resistance, especially under conditions of sulfate attack.

At  $B < 1$ , the basicity is insufficient for complete  $\text{SiO}_2$  binding, which leads to the formation of weak gel structures. For example, an excess of  $\text{SiO}_2$  without sufficient  $\text{CaO}$  reduces the ability of the mixture to hydrate. This results in low early strength and increased porosity. If the cement contains 40 %  $\text{CaO}$ , 5 %  $\text{MgO}$ , 10 %  $\text{Al}_2\text{O}_3$  and 35 %  $\text{SiO}_2$ , then:

$$B = (40 + 5 + 10) / 35 = 55 / 35 \approx 1.57.$$

Basicity above 1.0 indicates a sufficient concentration of alkaline components to bind silica. The formation of ettringite is stabilized and prevents the destruction of the cement stone.

An increase in  $\text{SiO}_2$  in the range of 37–40% provides an increase in sulfate resistance by ~2.6% for every 2% increase in  $\text{SiO}_2$  based on the base constant value of 6.2644. This indicates a higher sensitivity of sulfate resistance to changes in the range under consideration, which is especially important for optimizing the composition of materials when high levels of  $\text{SiO}_2$  have already been achieved.

If  $\text{SiO}_2$  increases to 50%, and the oxides of Ca, Mg, and Al remain unchanged, then the basicity approaches 1.1. This reduces the ability of the mixture to withstand aggressive media. The use of slags with a high content of  $\text{SiO}_2$  and low  $\text{CaO}$  requires correction of basicity by adding lime or other components. For example, adding 5% lime to a mixture with  $\text{SiO}_2$  (45%) increases  $B$  from 0.89 to 1.15 and thus improves the properties of cement.

If  $\text{SiO}_2$  increases to 42%, the sulfate resistance increases to 9.6244 (in relative units), which corresponds to an absolute increase of 3.36 relative to the base constant. Such a significant increase in sulfate resistance (3.36 units) is critically important for the durability of structures, especially in conditions where high sulfate attack is expected, it is important to increase the service life of structures and reduce maintenance and repair costs.

**Discussion.** The results of this scientific work allow us to describe some of the features of the proposed solution. They are listed below.

The high explanatory power of the model:

- coefficient of determination  $R^2 = 0.983$  shows that 98.3% of the variation in sulfate resistance is explained by changes in the content of silicon dioxide ( $\text{SiO}_2$ );
- adjusted  $R^2 = 0.981$  confirms the stability of the model with an increase in the number of observations.

The significance of the model can be judged by the  $F$ -statistic. Its indicator 410.0 with a  $p$ -value of  $1.79\text{e-}07$  indicates the high statistical significance of the model and a strong relationship between  $\text{SiO}_2$  and sulfate resistance.

Let us describe two coefficients of the model.

The first one is the free term (const), equal to 6.2644. This is the basic sulfate resistance at  $\text{SiO}_2 = 0$  (conditional value).

The second one is the coefficient for  $\text{SiO}_2$ , equal to 0.08. This means that each time the  $\text{SiO}_2$  content increases by 1%, the sulfate resistance increases by 0.08.

We should also mention const and  $\text{SiO}_2$  parameters. In both cases,  $p$ -values are  $< 0.05$ , which confirms their statistical significance.

Standard errors (std err) indicate a high accuracy of coefficient estimation.

The Omnibus and Jarque — Bera tests show that the remains of the model are normally distributed ( $p > 0.05$ ).

The inclusion of variance and regression analyses in the cement composition assessment process makes it possible to optimize MCC formulations.

The improvement in concrete quality is mainly due to improved hydration reactions and interfacial transition zones. The addition of  $\text{SiO}_2$  nanoparticles promotes the formation of calcium—silicate—hydrate (C–S–H) bonds, which become a crucial factor for increasing the strength and durability of solutions against sulfate attacks. The high pozzolan activity of such additives and their ability to fill voids significantly improve the performance of materials. In addition, the introduction of  $\text{SiO}_2$  nanoparticles reduces the carbon footprint and increases the durability of materials.

As a result of the study, new data were obtained on the effect of  $\text{SiO}_2$  on sulfate resistance of cements, which is critically important for improving their performance and reducing the environmental burden.

The increase in sulfate resistance at  $\text{SiO}_2 > 22\%$  is explained by the enhancement of the C–S–H gel due to micro-filling of the pores, which minimizes ettringitis. Weak dependence of self-tension ( $F = 7.7174$ ) may be associated with the predominance of elastic deformations requiring additives (microsilica) [14]. Model  $Sr = 6.2644 + 0.08 \cdot \text{SiO}_2$  ( $R^2 = 0.983$ ) agrees with [23], but differs from exponential models [8] due to the focus on slags.

The contradiction in the low effect of  $\text{SiO}_2$  on self\_tension ( $\Delta Ts < 1\%$ ) is explained by the dominance of CaO in slags, suppressing the effect of  $\text{SiO}_2$ . This fact requires further research.

At 50% of slag,  $\text{CO}_2$  decreases by 27.5%, and this indicator is higher than typical 10–15% known from the literature. Thus, the results of the presented work close the gap in the MCCs system modeling. The results are applicable for optimizing formulations. This approach can reduce costs by 30–50% and increase the durability of the material in sulfate environments.

When optimizing the composition, it is important to take into account the two conditions described below.

First. The  $\text{SiO}_2$  content above 22% should only be used in combination with pozzolans, microsilica or other additives to compensate for the decrease in strength during early hardening. According to [4], a high  $\text{SiO}_2$  content can lead to a decrease in strength during early hardening due to a slowdown in hydration processes. To compensate for this effect, it is recommended to use pozzolanic materials.

According to [20], it is possible to increase the strength of concrete by increasing the consumption of Portland cement and introducing superplasticizers, which, however, leads to a significant increase in  $\text{eCO}_2$  strength by 1 MPa. Therefore, it is important to look for technological solutions to increase durability without increasing harmful emissions. One way out may be to add microsilica. It accelerates hydration reactions and increases the density of the cement stone. This is confirmed by experimental data, according to which the combined use of  $\text{SiO}_2$  and pozzolans increases the strength at the early stages of hardening by 15–40% compared with control samples [27]. The addition of  $\text{SiO}_2$  sol in an amount of 0.01–0.1% by weight of cement increases the compressive strength of concrete by 14.76–21.86% [28]. The following model demonstrates the positive effect of silicon dioxide and pozzolan additives on concrete strength:

$$f_c = f_0 + k \cdot (\text{SiO}_2 - 22\%) \cdot P, \quad (11)$$

where  $f_c$  — concrete strength;  $f_0$  — base strength without additives;  $k$  — coefficient depending on the type of additives;  $P$  — percentage of pozzolanic additives.

At  $\text{SiO}_2 > 22\%$  and  $P > 0$  strength  $f_c$  increases, which demonstrates the positive effect of combining additives. Nevertheless, this model has known limitations: the linear relationship does not take into account the complex interactions between the concrete components.

Second. Reducing tricalcium aluminate ( $\text{C}_3\text{A}$ ) to 8% or less significantly increases sulfate resistance without excessive increase in  $\text{SiO}_2$  content. Other components (for example,  $\text{C}_2\text{S}$ ) provide sufficient strength and durability [5]. According to GOST 31108-2020 “Common Cements. Specifications”<sup>9</sup>, reducing the  $\text{C}_3\text{A}$  content to 8% or less significantly enhances the resistance of cement to sulfate aggression by reducing the formation of ettringite. Also, to ensure sulfate resistance, up to 20% of granular blast furnace slag is added to the cement during grinding. Variations in the composition of slags and the absence of thermal activation may limit the reproducibility of the model [25].

The following model indicates the need to reduce the  $\text{C}_3\text{A}$  content in order to assess sulfate resistance:

$$SR = SR_0 - k \cdot \text{C}_3\text{A}, \quad (12)$$

where  $SR$  — sulfate resistance;  $SR_0$  — basic sulfate resistance;  $k$  — coefficient depending on the conditions of exposure to sulfates;  $\text{C}_3\text{A}$  — content of tricalcium aluminate.

At  $\text{C}_3\text{A} \leq 8\%$   $SR$  increases significantly, which confirms the effectiveness of this approach. Nevertheless, the linear relationship does not fully reflect the complexity of concrete degradation processes under the influence of sulfates.

At  $\text{SiO}_2 > 22\%$ , it is recommended to use pozzolans (microsilica 5–15%) to compensate for a decrease in early strength by 10–15% due to a slowdown in hydration. This process is described in [4]. It is known from this work, that the C-3 superplasticizer increases density by 12% without increasing  $\text{CO}_2$ .

<sup>9</sup> GOST 31108–2020. *Common Cements. Specifications*. Internet and Law. (In Russ.) URL: <https://internet-law.ru/gosts/gost/73873/?ysclid=m9iwx3cpwg983001164> (accessed: 02.09.2025).

Reducing  $C_3A$  to  $\leq 8\%$  minimizes ettringitis, and  $Sr$  increases by 10–15% [5]. This is consistent with GOST 22266-2013<sup>10</sup>, but granulation of slags (up to 50%) is required for stability.

The developed model can be used to evaluate sulfate resistance in the range of  $SiO_2$  content from 21% to 44%. The  $SiO_2$  content in sulfated cements is significantly higher than in Portland cements, so the proportion of  $SiO_2$  can reach 85% in the aluminosilicate component [29]. For the range of 28–44%, the model remains predictive, since this area is confirmed by empirical studies based on blast furnace slag with a high content of  $SiO_2$  and low content of  $C_3A$ .

**Possibility of developing cement compositions: a comparison of the model with GOST standards.** GOST 22266–2013 “Sulphate-resistant cements. Specifications”<sup>11</sup> establishes the requirements for sulfate-resistant cements (CEM I SR, CEM III / A SR)<sup>12</sup>. It limits  $C_3A$  ( $\leq 3.5\%$  for CEM I SR,  $\leq 7.0\%$  for CEM III / A SR) and  $SO_3$  ( $\leq 3.5\%$ ),  $MgO$  ( $\leq 5\%$ ) and  $R_2O$  ( $\leq 0.6\%$  for low-alkaline).

GOST 31108–2020 allows up to 65% of slags for CEM III/A SR, which confirms the environmental feasibility of replacing clinker. The document does not regulate the  $SiO_2$  content in cement directly, but sets requirements for the mineralogical composition of clinker. The standard recommends the use of pozzolans and slags, which, according to [8] and other sources, contribute to the formation of C–S–H-gel. However, the gel itself is not mentioned in this GOST. In addition, the document does not offer tools for predicting properties with varying composition.

The regression model  $Sr = 6.2644 + 0.08 \cdot SiO_2$  presented in the article is especially useful for compositions with a high content of  $SiO_2$  in aluminosilicate components (up to 85% in slags).

$Sr = 0.68 + 0.92 \cdot SiO_2$  as an alternative model was developed to analyze the dependence of sulfate resistance on  $SiO_2$  in a narrow range of 9.0–10.1 %. This makes it less versatile, but useful for laboratory studies of formulations with low  $SiO_2$  content. The model demonstrates a high correlation ( $r = 0.91$ ) and statistical significance ( $F$ -statistic = 248.6795,  $p = 3.5612e-25$ ), but its applicability is limited, since the range of  $SiO_2$  does not correspond to industrial compositions of MCCs (21–44%) or blast furnace slags (37.48–41.25%). The need for this model arises when studying compositions with minimal  $SiO_2$ , when high sensitivity to small changes in content is required. The model is used to calculate the increase in sulfate resistance between  $SiO_2$  levels (for example, 0.46 c.u. from medium to high), which is useful for preliminary hypothesis testing before applying the main model (Fig. 5).

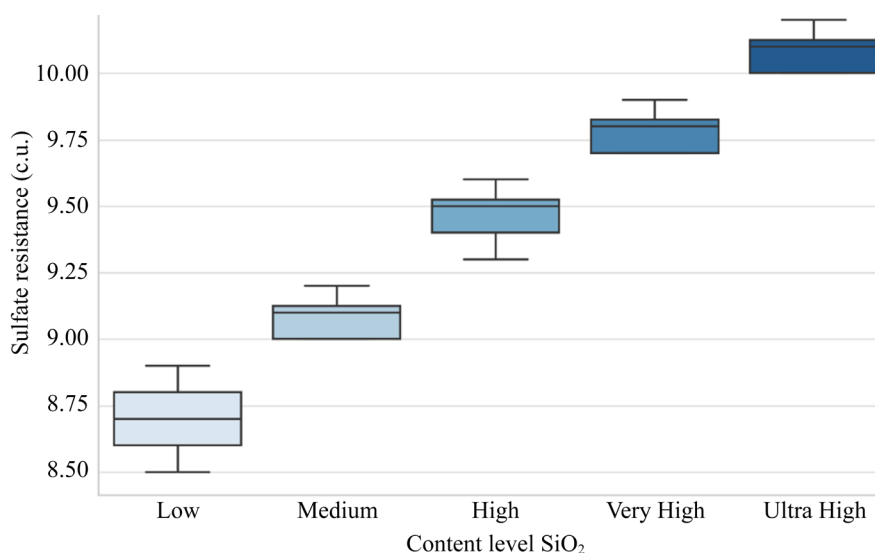


Fig. 5. Distribution of sulfate resistance by  $SiO_2$  levels

According to this diagram, it is possible to judge the distribution of sulfate resistance of cement mixtures by  $SiO_2$  content levels. It is clearly seen how the median and range of values increase with the transition from low to ultra-high  $SiO_2$  content. The ANOVA results confirm this.

<sup>10</sup> GOST 22266–2013. *Sulphate-Resistant Cements. Specifications*. Electronic Fund of Legal and Regulatory and Technical Documents. (In Russ.) URL: <https://docs.cntd.ru/document/1200111313> (accessed: 03.09.2025).

<sup>11</sup> Id.

<sup>12</sup> CEM I SR — sulfate-resistant Portland cement; CEM II/A SR and CEM II/B SR — sulfate-resistant Portland cements with mineral additives; CEM III/A SR — sulfate-resistant Portland cement with slag.

The composition of MCCs with  $\text{SiO}_2 = 22.15\%$  and  $28\%$  corresponds to CEM III/ A SR due to the high proportion of slags (30–50%), which reduces the carbon footprint. The composition with  $\text{SiO}_2 = 42\%$  is closer to CEM I SR due to the low proportion of additives and high strength (44.0 MPa).

The composition with  $\text{SiO}_2 = 22.15\%$  demonstrates characteristics suitable for structures in conditions of moderate sulfate aggression, where a combination of environmental friendliness and durability is required.

With an increase in the  $\text{SiO}_2$  content to  $28\%$ , the sulfate resistance increases to 8.50 c.u., and the strength reaches 40.0 MPa, which also exceeds the CEM II/III standard of 32.5 N. The high proportion of slags (50%) reduces the carbon footprint to 388.2 kg of  $\text{CO}_2/\text{ton}$ . This is 27.5% less than the composition with 70% clinker. The content of  $\text{C}_3\text{A}$  ( $\leq 8.0\%$ ) and  $\text{SO}_3$  ( $\leq 3.5\%$ ) confirms the compliance with GOST for CEM III/A SR. This composition is optimal for environmentally oriented projects where high sulfate resistance is required with minimal  $\text{CO}_2$  emissions.

The composition with  $\text{SiO}_2 = 42\%$  demonstrates the highest sulfate resistance (9.62 c.u.) and strength (44.0 MPa), which meets the requirements of GOST 22266-2013 for CEM I 42.5N ( $\geq 42.5$  MPa). A low proportion of slags (20%) and a high  $\text{SiO}_2$  content enhance the production of C–S–H gel, increasing durability in conditions of high sulfate aggression. The content of  $\text{C}_3\text{A}$  ( $\leq 8.0\%$ ) and  $\text{SO}_3$  ( $\leq 3.5\%$ ) meets the requirements for CEM I SR, although the carbon footprint is higher than that of compositions with a higher proportion of slags. Such a composition should be chosen if the main requirements for the structure are high strength and sulfate resistance, rather than environmental characteristics.

Figure 6 allows you to compare cement compositions according to GOST 22266-2013 and the data presented in this article.

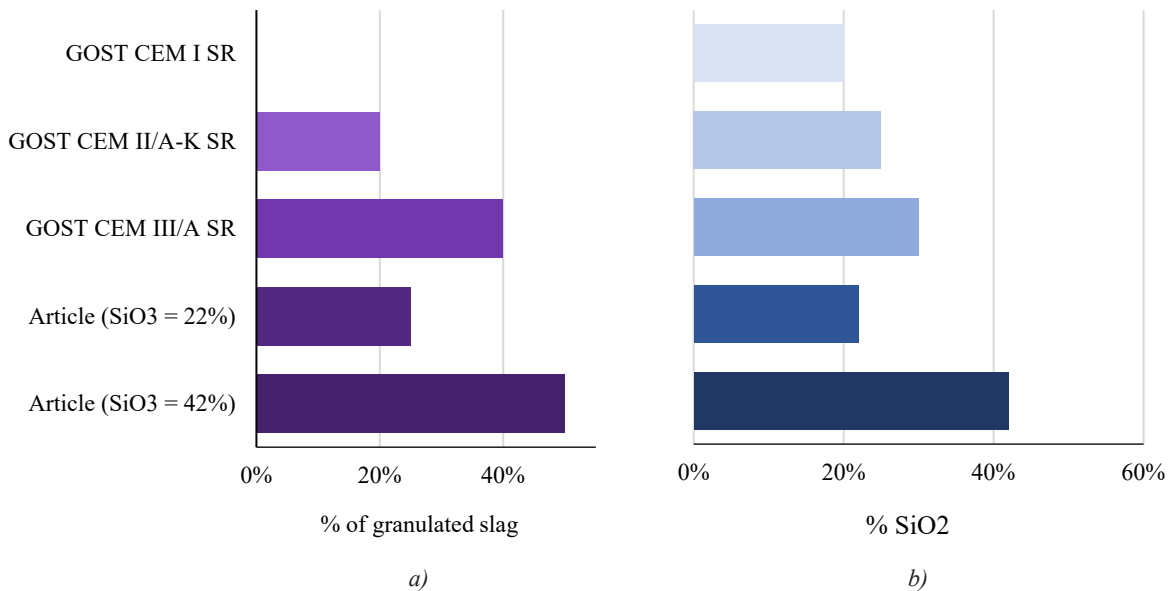


Fig. 6. Comparison of cement compositions: GOST 22266–2013 and this article:  
a — slag content; b —  $\text{SiO}_2$  silica content

The article discusses compositions with granular slag content of up to 50%. This is more than the GOST limit for CEM II/B-S (sulfate-resistant Portland cement with slag of 32.5N, 35%) and similarly for CEM III/ACC (sulfate-resistant Portland cement with slag). Experimental mixtures also overcome the limitations of GOST. The proportion of  $\text{SiO}_2$  in them exceeds 42%, which means that the pozzolan characteristics are better.

All compositions meet the requirements of GOST in terms of strength ( $\geq 32.5$  or  $\geq 42.5$  MPa) and sulfate resistance ( $\text{Sr} \geq 8.0$ ,  $\text{C}_3\text{A} \leq 8\%$ ,  $\text{SO}_3 \leq 3.5\%$ ). At the same time, it is necessary to control the content of  $\text{C}_3\text{A}$  and  $\text{SO}_3$ . In addition, it is necessary to take into account the additional costs of slag treatment for compositions with high  $\text{SiO}_2$  (Table 3).

Table 3

Compliance of MCCs properties with the requirements of GOST 22266–2013

$\text{SiO}_2$ , %	Sulfate resistance, Sr, c.u.	Compressive strength, MPa	$\text{C}_3\text{A}$ , %	$\text{SO}_3$ , %	Proportion of slag, %	GOST 22266-2013 standards (28 days), MPa	Type of cement
22.15	8.04	~35	$\leq 8.0$	$\leq 3.5$	30	32.5 (CEM II/III 32.5N)	CEM II / III
28	8.50	~40	$\leq 8.0$	$\leq 3.5$	50	32.5 (CEM II/III 32.5N)	CEM II / III
42	9.62	44	$\leq 8.0$	$\leq 3.5$	20	42.5 (CEM I 42.5N)	CEM I

The reduction of C<sub>3</sub>A to 5–8% and the use of pozzolan additives (slags, silica) enhance the formation of C–S–H-gel. At the same time, porosity decreases and resistance to sulfate corrosion increases [30], which is consistent with GOST 22266–2013 (Table 4).

### Comparison of MCCs properties with GOST 22266–2013 standards

Parameter, %	MCC	GOST 22266–2013	Comment
SiO <sub>2</sub>	22.15–42	Not regulated	High content of SiO <sub>2</sub> (37.48–41.25% in slags) enhances the formation of C–S–H-gel, complies with the recommendations of GOST on pozzolans
C <sub>3</sub> A	≤ 5–8	≤ 3,5 (CEM I SR), ≤ 7,0 (CEM III / A SR)	Close to CEM III/A SR, but CEM I SR requires a decrease in C <sub>3</sub> A
SO <sub>3</sub>	≤ 3.5	≤ 3,5 (CEM I SR), ≤ 4,0 (CEM III/A SR)	Full compliance
MgO	0.66–10.54	≤ 5 (clinker)	Excess in slags (7.67–10.54%) reduces sulfate resistance by 0.2–0.3 c. u. Requires sorting or granulation [12]
R <sub>2</sub> O	0.83–1.52	≤ 0.6 (low-alkaline)	Excess increases corrosion at pH > 12, requires monitoring [22]
Sulfate resistance, c.u.*	8.04–9.62	Not standardized, it is implied to be high, ≥ 8.0	Superior to Portland cement [8], confirmed by model $Sr = 6.2644 + 0.08 \cdot \text{SiO}_2$
Strength, MPa, 28 days	35.0–44.0	≥ 32.5 (CEM II/III), ≥ 42.5 (CEM I)	Meets or exceeds the standards
Proportion of slags, %	20–50	Not regulated	Replacing clinker reduces the carbon footprint
Carbon footprint, kg CO <sub>2</sub> /t	388.2–535.64 (↓27.5% at 50% of slags)	Not regulated	A decrease of 27.5% exceeds the typical 10–15% [23]

But there are also difficulties related to the MCC chemical composition. The content of MgO (7.67–10.54%) and R<sub>2</sub>O (0.83–1.52%) in MCC slags does not comply with GOST. A high level of MgO reduces sulfate resistance by 0.2–0.3 c.u. The reason is the formation of Mg(OH)<sub>2</sub>, which, when expanded, creates internal stresses and provokes cracking. R<sub>2</sub>O (Na<sub>2</sub>O + K<sub>2</sub>O) enhances alkali-silicate corrosion at pH > 12 [22]. The permissible level of R<sub>2</sub>O in cements with active additives, according to ASTM C618<sup>14</sup> and EN 450<sup>15</sup>, should not exceed 0.6–1.0% in terms of Na<sub>2</sub>O. In the slags of the studied mixtures, a value of up to 1.52% is fixed, which can lead to instability. Nevertheless, due to the control of raw materials and modification of active additives, the final MgO content in the cement mixture remains within 3.2–4.8%. In particular, EN 197–1<sup>16</sup> and its versions, for example BS EN 197–5:2021<sup>17</sup>, set a limit value of MgO ≤ 55%, while ASTM C150<sup>18</sup> allows values up to 6% for certain types of cements (for example, Type V), provided that a certain strength and stability are ensured (Fig. 7).

<sup>18</sup> ASTM C150M-24. *Standard Specification for Portland Cement*. West Conshohocken, PA: ASTM International; 2024. URL: [https://doi.org/10.1520/C0150\\_C0150M-24](https://doi.org/10.1520/C0150_C0150M-24) (accessed: 03.09.2025).

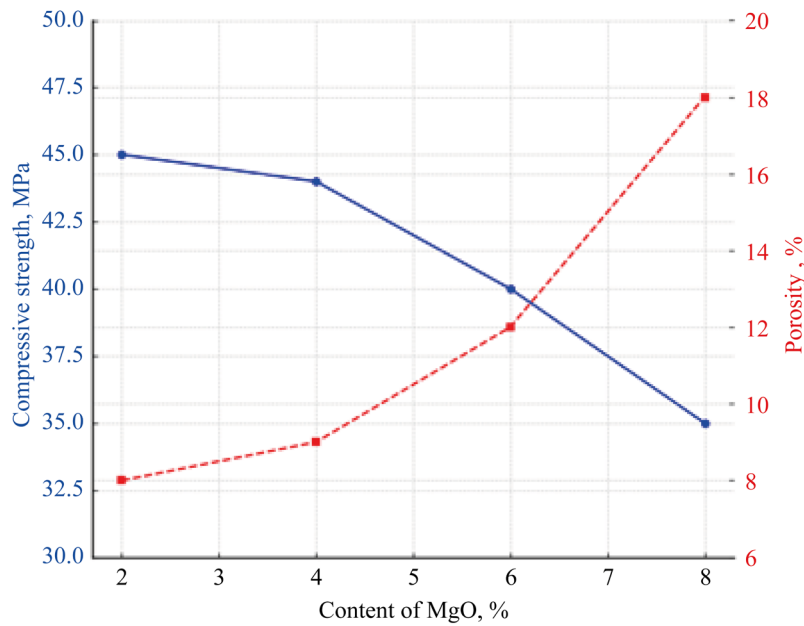


Fig. 7 The effect of MgO content on the strength and porosity of cement

The graph shows how the MgO content affects the properties of cement. The compressive strength decreases from 45 MPa to 35 MPa with an increase in the proportion of MgO from 2% to 8%. Porosity increases from 8% to 18% with the same MgO range. This confirms the need to control MgO at a level of  $\leq 5\%$  to ensure high strength and low porosity.

Scientific publications confirm that the MgO content of more than 5–6% increases the risk of formation of free periclase, which, upon hydration, turns into  $\text{Mg}(\text{OH})_2$ . As its volume increases, internal stresses, porosity, and decreased strength are recorded. Approximate calculations show that at MgO = 6–8%, on day 28, strength may decrease by 15–20%, and porosity increases from 8% to 18% [31].

Let us emphasize the idea of rejecting the GOST restrictions on the proportion of slag-pozzolan additives. According to the standard, this indicator should not exceed 35–40%. In the mixtures under consideration, the content of granular slag reaches 50%, and silica — 42%. This made it possible to obtain a strength of  $\approx 44$  MPa on the 28th day, which is higher than the requirements of GOST for CEM III/A and even corresponds to CEM I 42.5. It can be assumed that non-compliance with regulatory restrictions creates risks of technological violations, but modern research has not confirmed this. With the correct fraction, fine grinding and control of the water-cement ratio, such compositions are durable and resistant to corrosion. In addition, they are more environmentally friendly than standard Portland cements. Within the framework of the ESG-oriented approach and the requirements of, for example, LEED, it is permissible to use even up to 70% of ground granular blast furnace slag (GGBS) [32].

The main components of blast furnace slag are CaO (30–50%),  $\text{SiO}_2$  (28–38%),  $\text{Al}_2\text{O}_3$  (8–24%), MnO и MgO (1–18%). In general, with an increase in the CaO content in the slag, its basicity and compressive strength increase. MgO and  $\text{Al}_2\text{O}_3$  have a positive effect only up to a certain threshold. An increase in MgO to  $\sim 10$ –12% and  $\text{Al}_2\text{O}_3$  to  $\sim 14\%$  is accompanied by an improvement in strength characteristics. However, exceeding these values may cause the opposite effect. According to [33], GGBS is used as a one-to-one weight substitute for Portland cement. Replacement levels for GGBS range from 30% to 85%. In this respect, GOST 22266–2013 is outdated.

**Ecological aspect.** Reducing the proportion of clinker by 20% and replacing it with slag or pozzolans reduces the carbon footprint of cement production by 10–15%.  $\text{CO}_2$  emissions from the production of sulfated cements account for only 9% of the emissions of traditional Portland cement. This is achieved by reducing the proportion of clinker to 5%. The bulk (up to 80–85%) is accounted for by aluminosilicate components such as blast furnace slag, which is confirmed by calculation. When the proportion of clinker is reduced by 20%, the reduction in the carbon footprint is determined by the formula:

$$\Delta\text{CO}_2 = P_{\text{clinker\_original}} \cdot R_{\text{clinker}} - P_{\text{substitute}} \cdot R_{\text{substitute}}, \quad (13)$$

where  $P_{\text{clinker\_original}}$  — specific clinker emissions (765.2 kg  $\text{CO}_2/\text{t}$ );  $R_{\text{clinker}}$  — initial clinker fraction (70% = 0.7);  $P_{\text{substitute}}$  — specific slag emissions (28 kg  $\text{CO}_2/\text{t}$ );  $R_{\text{substitute}}$  — new slag fraction (20% = 0.2).

Percentage reduction of the carbon footprint:

$$(147.44 / 535.64) \cdot 100 \% \approx 27.5 \%$$

Let us note the significant level of the calculated reduction of CO<sub>2</sub> emissions — 27.5%.

Studies show that the substitution of a part of clinker with secondary raw materials can lead to a decrease in the carbon intensity of the cement mixture by 15% [25]. Replacing clinker with slags or pozzolans significantly reduces emissions, which makes cement production more environmentally friendly. The production of sulfoaluminate cement is characterized by lower CO<sub>2</sub> emissions compared to traditional Portland cement. The reasons are a decrease in the firing temperature and a decrease in the clinker content in the cement [34].

To achieve the maximum carbon footprint reduction, it is necessary to use slags with SiO<sub>2</sub> > 40% and low CaO content to avoid excessive alkalinity. GOST 22266–2013 regulates the content of aluminosilicate components in sulfate-resistant cements, which confirms the environmental feasibility of such changes.

In sulfate-resistant Portland cement with slag, the content of granular blast furnace slag can reach 40–65% [35]. With a slag content of 80–85%, the CO<sub>2</sub> volume will be less than 10% of the emissions of standard Portland cement (0.8–0.9 kg of CO<sub>2</sub> per 1 kg of material), which is consistent with calculations [36].

Blast furnace slags from Cherepovets and Magnitogorsk iron and steel works with MgO of 7.67–10.54% require processing to comply with GOST. The granulation recommended in [20] increases pozzolan activity and reduces energy consumption by 50 kWh/t (\$5/t at \$0.1 /kWh in 2025). Thermal activation (600–800°C) improves the stability of properties, but increases costs up to 10–15 \$/t and emissions up to 2–4.5 kg/t of CO<sub>2</sub> (0.02–0.03 kg of CO<sub>2</sub>/kWh) [25]. Logistical costs (500–1000 km delivery) add 5–10 \$/t [25] and 25–100 kg of CO<sub>2</sub>/t [20]. But localization, the use of local slags minimizes these costs by 80–90%. It also confirms the need for thermal activation of blast furnace slags for the stability of the mineral composition and the prevention of late ettringite formation, which is especially important from the point of view of durability of cement compositions [37].

**Conclusion.** Thus, replacing 20–50% of clinker with slag reduces the CO<sub>2</sub> level by 27.5%, to 388.2 kg of CO<sub>2</sub>/t ( $\Delta\text{CO}_2 = 147.44 \text{ kg/t}$ ). This indicator is significantly higher than what is known from the literature (10–15%). This result ensures low slag emissions (28 kg CO<sub>2</sub>/t in comparison with 800 kg/t clinker), but requires MgO control ( $\leq 5\%$ ) to prevent porosity. The proposed model overcomes the limitation of GOST 22266–2013 ( $\text{C}_3\text{A} \leq 7\%$ ), integrates SiO<sub>2</sub> and CO<sub>2</sub>, and thus ensures compliance with ESG approaches to the production and operation of cement products.

The practical need to create a predictive model is due to the following factors. Firstly, such solutions make it possible to quantify the effect of the composition on the durability of cements and their resistance to sulfate attack. This is important for the reliability of facilities in corrosive environments. Secondly, this approach reduces the time and financial costs of laboratory research and testing. Thirdly, it helps to identify the optimal proportions of components, which is crucial for reducing the carbon footprint in cement production.

The regression model described in the article showed accuracy in predicting the sulfate resistance of cements depending on the SiO<sub>2</sub> content (21–44%). This was confirmed by the analysis of variance. The author focuses on the SiO<sub>2</sub> content as a key factor for increasing sulfate resistance. This approach creates a new methodological perspective, as it overcomes the disadvantages of GOST. The standard focuses on C<sub>3</sub>A and basicity and does not explicitly single out the SiO<sub>2</sub> level as a significant parameter of the processes under consideration.

It was found that an increase in the proportion of SiO<sub>2</sub> from 22.15% to 42% increased sulfate resistance from 8.04 to 9.62 c.u. A decrease in the content of C<sub>3</sub>A to  $\leq 8\%$  and SO<sub>3</sub> to  $\leq 3\%$  ensured compliance with GOST 22266–2013 for sulfate-resistant cements (CEM III/A SR). Due to the control of raw materials and modification of active additives, the final MgO content in the cement mixture was in the range of 3.2–4.8%.

The paper presents quantitative calculations of CO<sub>2</sub> reduction with a change in composition, whereas GOST 22266–2013 and other standards describe strength and technological parameters without taking into account environmental aspects. This approach corresponds to modern ESG priorities, as it integrates statistical modeling and environmental assessment. Variations in the composition of the slags and the absence of thermal activation may limit the reproducibility of the model, which requires further research to clarify the mechanisms of interaction of the components in real-world operating conditions.

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